

## ISO Update

Who knew standardization could be this fun?

Léo Perrin

Inria, France

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**Dagstuhl 20041**



How are **Streebog** and **Kuznyechik** doing?



## Outline

- 1 General Context
- 2 "Randomness" of a Structure: The Kolmogorov Anomaly
- 3 "Counter Arguments"
- 4 Conclusion

## Plan of this Section

- 1 General Context
  - What are these Algorithms?
  - Timeline and Results
  - What the Designers Say
- 2 "Randomness" of a Structure: The Kolmogorov Anomaly
- 3 "Counter Arguments"
- 4 Conclusion

# Kuznyechik/Streebog

## Streebog

Type Hash function

Publication 2012

## Kuznyechik

Type Block cipher

Publication 2015



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## Common ground

- Both are standard symmetric primitives in Russia.
- Both were designed by the FSB (TC26).
- Both use the same  $8 \times 8$  S-Box,  $\pi$ .

# Timeline

By **March 2016**, Kuznyechik and Streebog were both **GOST** standards and **IETF RFCs**.

**May 2016** Publication of the first decomposition (TU-decomposition) EC'16

**Feb 2017** Publication of the second decomposition (Belarus-like) FSE'17

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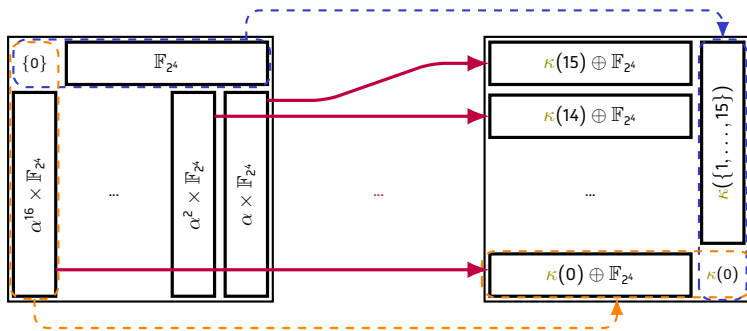
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**Summer 2019** **Time to act**

**Oct. 2019** ISO had to make a decision

# The TKlog Structure

$$\pi : \begin{cases} \mathbb{F}_{2^8} & \rightarrow \mathbb{F}_{2^8} \\ 0 & \mapsto \kappa(0) \\ \alpha^{17j} & \mapsto \kappa(16 - j) & \text{for } 1 \leq j \leq 15 \\ \alpha^{i+17j} & \mapsto \kappa(16 - i) \oplus (\alpha^{17})^{s(j)} & \text{for } 0 < i, 0 \leq j < 16 \end{cases}$$



# RUnet

The use of national encryption standards is being made **mandatory** in Russia.

[https://www.cnews.ru/news/top/2019-04-02\\_vlasti\\_prinuditelno\\_perevedut\\_runet\\_na\\_rossijskie](https://www.cnews.ru/news/top/2019-04-02_vlasti_prinuditelno_perevedut_runet_na_rossijskie)

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Рунет принудительно переводят на российские стандарты

← → cnews.ru/news/top/2019-04-02\_vlasti\_prinuditelno\_perevedut\_runet\_na\_rossijskie

**cnews**    НОВОСТИ    АНАЛИТИКА    КОНФЕРЕНЦИИ    РЫНОК    ТЕХНИКА    ТВ

Суть статьи: По оценкам специалистов, при этом ежегодные выплаты для поддержания работоспособности суверенного Рунета, по оценке специалистов Экспертного совета при правительстве России, могут достигать 134 млрд руб.

### Дополнение

После публикации этого материала представители компании «Инфотекс» обратились к CNews с просьбой опубликовать комментарий на тему недеklarированных возможностей в отечественных алгоритмах шифрования.

Если обратиться к первоисточнику по теме – статье **Лео Перрина**, то в ней дается только предположение о наличии алгоритма построения S-box, при этом сразу же, без каких-либо обоснований и примеров реализации атак на рассматриваемые криптоалгоритмы «Стрибог» и «Кузнечик», делается вывод о наличии в них недеklarированных возможностей, т.е. закладок. На наш взгляд, эта публикация носит явно спекулятивный характер и имеет своей целью срыв работ российских экспертов по продвижению указанных криптоалгоритмов в международные стандарты ИСО.

Для интересующихся темой хотим отметить, что построение надежного S-box является одной из важнейших и сложных задач современной криптографии. И ни в одном из принятых к использованию национальных, в т.ч. и стандартизованных криптоалгоритмов, включая AES и Кескал (SHA-3), S-box'ы не являются чисто случайной последовательностью. При выборе S-box анализируется целый ряд параметров: нелинейность, алгебраическая степень, алгебраическая иммунность и т.п. Все оптимизировать одновременно невозможно. Поэтому разрабатываются разные методы оптимизации и оценки стойкости, что в итоге и приводит к псевдослучайности выбранных S-box. Таким образом, такое свойство S-box следует считать нормой, а не чем-то аномальным, вокруг чего можно сразу выстроить множество «теорий заговора».

## What its Designers Said (at ISO)

questioned is the S-box  $\pi$ . This S-box was chosen from Streebog hash-function and it was synthesized in 2007. Note that through many years of cryptanalysis no weakness of this S-box was found. The S-box  $\pi$  was obtained by pseudo-random search and the following properties were taken into account.

[...]

No secret structure was enforced during construction of the S-box. At the same time, it is obvious that for any transformation a lot of representations are possible (see, for example, a lot of AES S-box representations).

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In private conversations, they explicitly said they used a Fisher-Yates shuffle to generate random S-boxes.



## Plan of this Section

- 1 General Context
- 2 “Randomness” of a Structure: The Kolmogorov Anomaly
  - Definition
  - How to Estimate It?
- 3 “Counter Arguments”
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## General Question

How "far" is the behaviour of a specific S-box from that of a "random S-box"?

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How likely is it for a random S-box to have a "structure"?

## Definition

```
p(x){unsigned char*k="@`rFTDVbpPB
vdtfRQ\xacp?\xe2>4\xa6\xe9{z\xe3q
5\xa7\xe8",a=2,l=0,b=17;while(x&&
(l++,a^x))a=2*a^a/128*29;return l
%b?k[l%b]^k[b+l/b]^b:k[l/b]^188;}
```

165 ASCII characters that fit on 7 bits: this program is 1155-bit long.

<https://codegolf.stackexchange.com/questions/186498/>

proving-that-a-russian-cryptographic-standard-is-too-structured

Let  $P(S)$  be the bitlength of a C implementation of  $S \in \mathfrak{S}_{2^n}$ .

### Definition (Kolmogorov Anomaly)

The **Kolmogorov Anomaly** of  $S$  for C is the opposite of the  $\log_2$  of the probability that a random S-box has a C implementation at most as long as that of  $S$ .

## Estimating the Kolmogorov Anomaly

How to estimate it?



- ( $\leq 1155$ )-bit C programs implementing 8-bit permutations
- ( $\leq 1155$ )-bit strings
- $\mathfrak{S}_{2^8}$

For  $\pi$ , we get:

$$\frac{\#(\leq 1155)\text{-bit C prog.}}{|\mathfrak{S}_{2^8}|} \leq \frac{\#(\leq 1155)\text{-bit strings.}}{|\mathfrak{S}_{2^8}|} = \frac{2^{1156} - 1}{256!} \approx 2^{-528},$$

meaning that the Kolmogorov anomaly of  $\pi$  for C is at least 528.

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  - Artist Rendition
  - Summary of the Counter-Arguments I Was Told
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## Artist Rendition



*Discussions with the Alleged Designers, Allegory.*  
Python M., 1969.

## An S-box is always like this (1/2)

- 1 Unfortunately, we lost the generation program so we can't show it to you
- 2 S-boxes always have a structure, why do you complain about this one and not about this AES?
- 3 If you optimize the differential/linear properties, a structure will appear
- 4 You are just a mathematician, in the *real world*<sup>TM</sup> we don't phase out algorithms unless we have an attack.

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<sup>1</sup>See excellent write up at <https://crypto.stackexchange.com/questions/75456/how-to-check-whether-the-permutation-is-random-or-not>



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*Quite convenient*
- 2 S-boxes always have a structure, why do you complain about this one and not about this AES?  
*No claims of randomness from the AES designers*
- 3 If you optimize the differential/linear properties, a structure will appear  
*Simply not true, it also does not match other anomalies<sup>1</sup>*
- 4 You are just a mathematician, in the *real world*<sup>TM</sup> we don't phase out algorithms unless we have an attack.  
*I never said I had an attack, but I do think lying is bad (even in the real world<sup>TM</sup>).*

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## An S-box is always like this (2/2)

- 5 There is something about C that allows you to find this implementation, it merely says something about the C language and not  $\pi$ .
- 6 There are all kind of 8-bit bijective S-box structures in the literature!

	Special polynomials	$2^{22}$
	Generation using paths (?)	$2^{255}$
†	TU <sub>4</sub> -decomposition (w/ mult)	$2^{88}$
→	TU <sub>4</sub> -decomposition (called "F-construction")	$2^{1417}$
†	Feistel 1r	$2^{64}$
	Feistel 1r (weird)	$2^{130}$
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	SPN 3r (Iceberg-like)	$2^{104}$
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	SPN 2r (Crypton v1)	$2^{152}$
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†	Lai-Massey (FLY-style)	$2^{152}$
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†	Perrin (neither mine nor a permutation)	$2^{304}$
	LFSRs	$2^{12}$
Total (with affine-equivalence)		$\approx 2^{1488}$

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*That's not even wrong.*

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$2^{1488}$  is in fact  $\approx 2^{196}$  times smaller than 256!  $\approx 2^{1683.996}$ .

# They Actually Said That (see ISO/IEC JTC 1/SC 27/WG2 N 2063)

## 2.3 Shift registers

One more way of substitution generation is shifting number  $x \in GF(2^8)$  by a linear feedback shift register (see Fig. 1) by a number of steps  $n \in \{0, 255\}$ . Since it is necessary that the substitution is full-round, the polynomial of degree 8, whose coefficients determine the feedback function, is required to be primitive. Then the number of substitutions is set by the choice of the number  $n$  and the number of primitive polynomials.

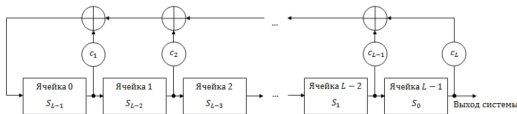


Figure 1

The number of polynomials over  $GF(2)$  is  $\frac{\varphi(2^8-1)}{8} = \frac{128}{8} = 16$ , so approximately  $2^8 \cdot 2^4 = 2^{12}$  substitutions may be obtained this way.

[...]

this word. Based on this remark we apply the affine transformation only to the output. The result is  $2^{1488}$  substitutions in total. And this size is approaching the total number of 16 element substitutions, which equals to  $256! \approx 2^{1683}$ .

## Best Argument

- 7 **Anti-Russia bias !!1!**  
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Except for the US

less than a year ago

who said the same thing

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## Conclusion

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IETF	<b>Good</b>	<b>Good</b>
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Thank you!

# Translation

(with thanks to google translate)

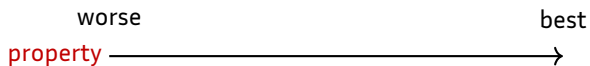
[...], representatives of the **Infotex company** asked CNews to publish a comment on the topic of undeclared capabilities in domestic encryption algorithms.

Leo Perrin's article [...] only **conjectures** that there is an algorithm for constructing an S-box, while immediately, without any justification and examples of attacks to "Stribog" and "Grasshopper", it is concluded that there are undeclared functionalities in them, i.e. backdoors. In our opinion, this publication is **clearly speculative** in nature and **aims** to disrupt the work of Russian experts in promoting these cryptographic algorithms in international ISO standards.

[...] in standard encryption algorithms, including AES and Keccak (SHA-3), **S-boxes are not purely random sequences**. When choosing an S-box, a number of parameters are taken into account: nonlinearity, algebraic degree, algebraic immunity, etc. [...] Thus, such an S-box property should be considered the norm, and not something abnormal, around which you can immediately build a lot of **"conspiracy theories."**

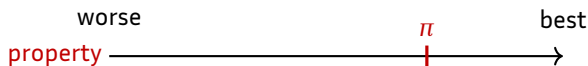
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### Negative Anomaly

$$\bar{\mathcal{A}}(\pi) = -\log_2 \left( \frac{\text{\#worse S-boxes}}{(2^n)!} \right)$$

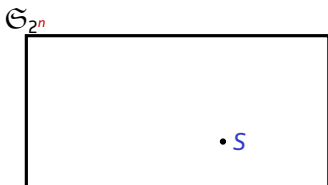
### Positive Anomaly

$$\mathcal{A}(\pi) = -\log_2 \left( \frac{\text{\#better S-boxes}}{(2^n)!} \right)$$

## Bad Idea: Using Instance-Tailored Properties

Let  $S \in \mathcal{S}_{2^n}$  be the studied S-box. We define a property  $P_S$  as

$$P_S : \begin{cases} \mathcal{S}_{2^n} & \rightarrow \mathbb{N} \\ F & \mapsto \# \{x \in \mathbb{F}_2^n, F(x) = S(x)\} . \end{cases}$$

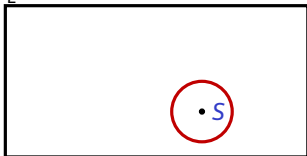




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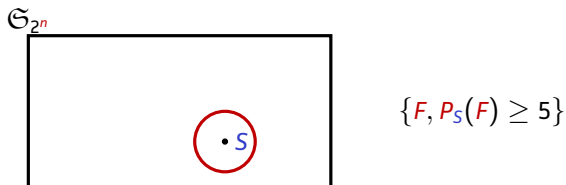
 $\mathcal{S}_{2^n}$ 


$$\{F, P_S(F) \geq 5\}$$

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The corresponding anomaly is useless: we can choose  $S$  arbitrarily!

## Experimental Results

Type	Cipher	Differential		Linear		Boomerang	
		$A^d(s)$	$\bar{A}^d(s)$	$A^\ell(s)$	$\bar{A}^\ell(s)$	$A^b(s)$	$\bar{A}^b(s)$
Inverse	AES	7382.1	0.00	3329.4	0.00	9000.1	0.0
TKlog	Kuznyechik	80.6	0.00	34.4	0.00	14.2	0.0
SPN (2S)	CLEFIA_S0	2.6	0.2	25.6	0.0	0.0	15.6
	Twofish_p0	1.4	0.7	3.2	0.2	0.0	33.8
Feistel	ZUC_S0	16.2	0.0	3.2	0.2	0.0	NaN
Hill climbing	Kalyna_pi0	104.2	0.0	235.8	0.00	29.7	0.00
Random	MD2	1.4	0.7	0.1	2.4	1.0	0.4
Unknown	Skipjack	0.2	1.9	54.4	0.0	1.0	0.4