

# SPLIT REGISTER ALLOCATION

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# OUTLINE

SPLIT COMPILATION

REGISTER ALLOCATION

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# INTRODUCTION

- Just-in-time (JIT) compilation has been introduced to ally:

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- Just-in-time (JIT) compilation has been introduced to ally:
  1. portability (interpretation)
  2. better performance (static compilation)

# SPLIT COMPILATION: MOTIVATION

## HARD OPTIMISATION PROBLEM:

- Exponential complexity algorithm
- Execution context dependent (data-set, target)

## DIFFICULTY:

1. Exploit information from expensive analysis
2. When execution context is known

## HOW TO ACHIEVE THESE GOALS SIMULTANEOUSLY?

# BEYOND ANNOTATION-ENHANCED JIT COMPILATION

1. Reducing dynamic compilation time [Krintz'01]
2. Improving performance of generated code [Jones'00]

# BEYOND ANNOTATION-ENHANCED JIT COMPILATION

1. Reducing dynamic compilation time [Krintz'01]
2. Improving performance of generated code [Jones'00]
3. **The goal** is to split complex and target-dependent optimisations into two **coordinated stages**: **offline** (static compiler) and **online** (JIT compiler)



# A CASE FOR SPLIT COMPILATION

Register allocation:

1. Have frequent accessed variables in processor's registers
2. One of the most profitable optimisation
3. It is not trivial to split and we will see why and how

# REGISTER ALLOCATION

- Graph Coloring framework [Chaitin'81], [Briggs'94]

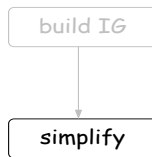
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- Graph Coloring framework [Chaitin'81], [Briggs'94]

build  $IG$

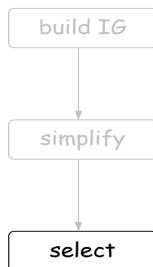
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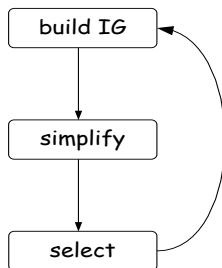
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# DECOUPLED REGISTER ALLOCATION

- [Appel'01], [Hack'06], [Bouchez'06]

## PROCEDURE

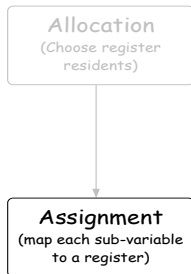
**Allocation**  
(Choose register  
residents)

## EXAMPLE

# DECOUPLED REGISTER ALLOCATION

- [Appel'01], [Hack'06], [Bouchez'06]

## PROCEDURE



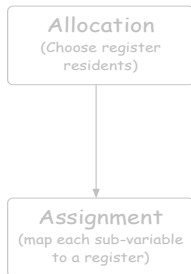
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## PROCEDURE



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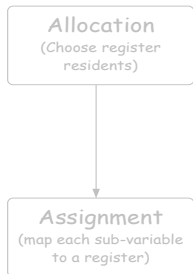
code

```
1: d = ...
2: b = load ...
3: b = b * d
4: a = load ...
5: a = d / a
6: c = a / b
7: a = b + c
8: store c
9: store a
```

# DECOUPLED REGISTER ALLOCATION

- [Appel'01], [Hack'06], [Bouchez'06]

## PROCEDURE



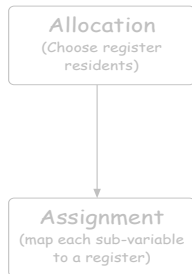
## EXAMPLE

code	live
1: d = ...	d
2: b = load ...	b, d
3: b = b * d	b, d
4: a = load ...	a, b, d
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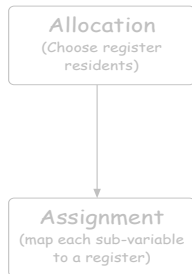
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code	live	
1: d = ...	d	1
2: b = load ...	b, d	2
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2 Available registers



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(Choose register residents)

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maxlive

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maxlive

a

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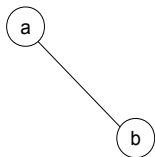
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maxlive



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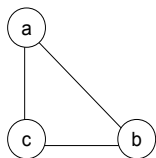
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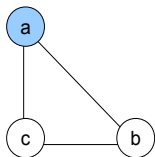
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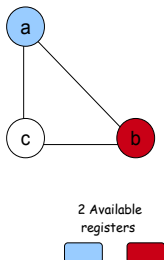
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**splitting**

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8: store c	a	1
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## PROCEDURE

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7: a3= b2 + c1	a3, c1	2
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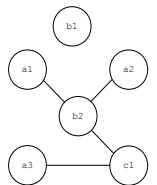
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**maxlive**



2 Available registers



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## PROCEDURE

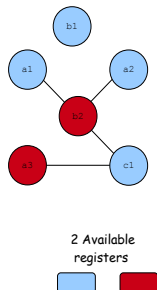
Allocation  
(Choose register residents)  
splitting

Assignment  
(map each sub-variable  
to a register)

## EXAMPLE

code	live	
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2: b1= load ...	b1, d	2
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5: a2= d / a1	a2, b2	2
6: c1= a2 / b2	b2, c1	2
7: a3= b2 + c1	a3, c1	2
8: store c1	a3	1
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maxlive



# GLOBAL VIEW OF SPLIT REGISTER ALLOCATION

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Allocation

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Allocation

maxlive

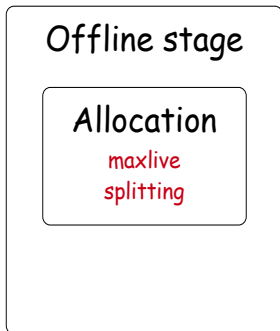
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Allocation

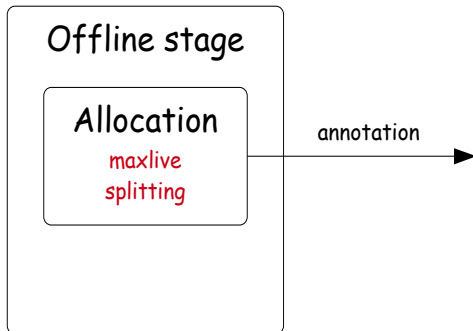
maxlive  
splitting



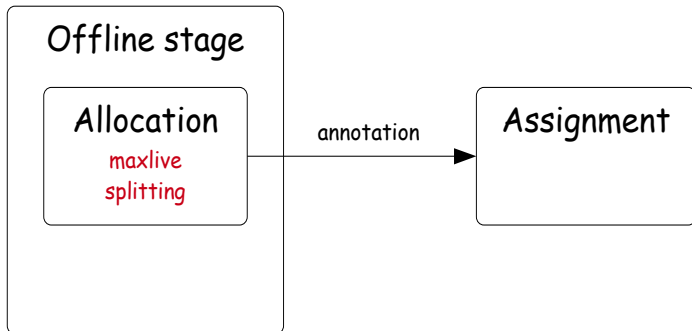
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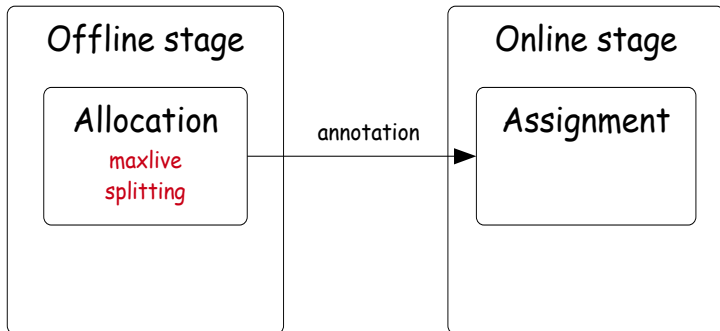
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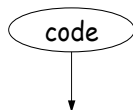


# STAGES OF SPLIT REGISTER ALLOCATION

code

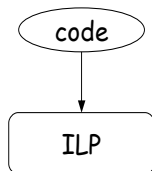
offline

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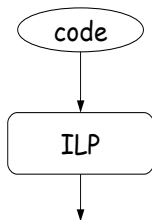
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offline

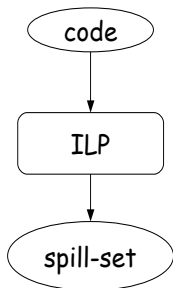
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offline

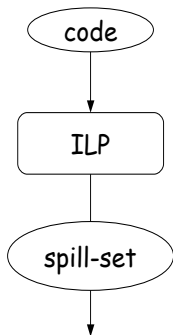


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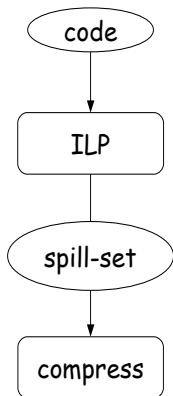
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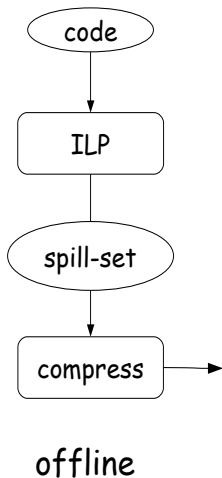
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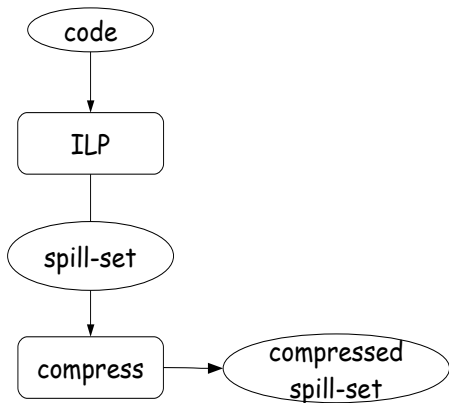


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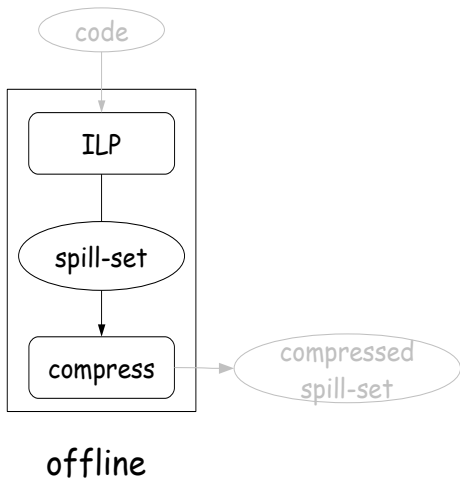


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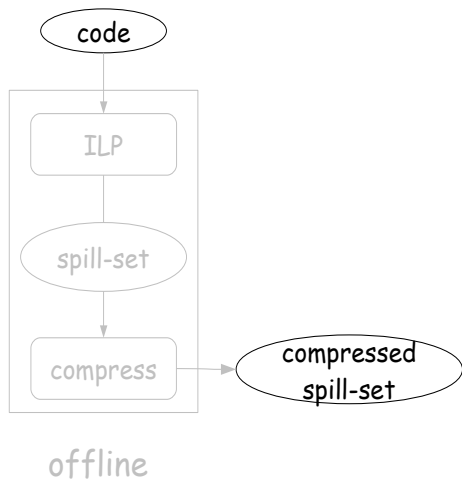


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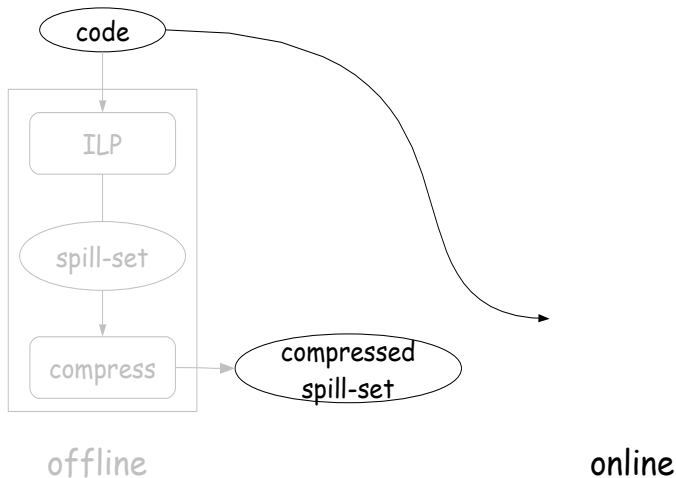
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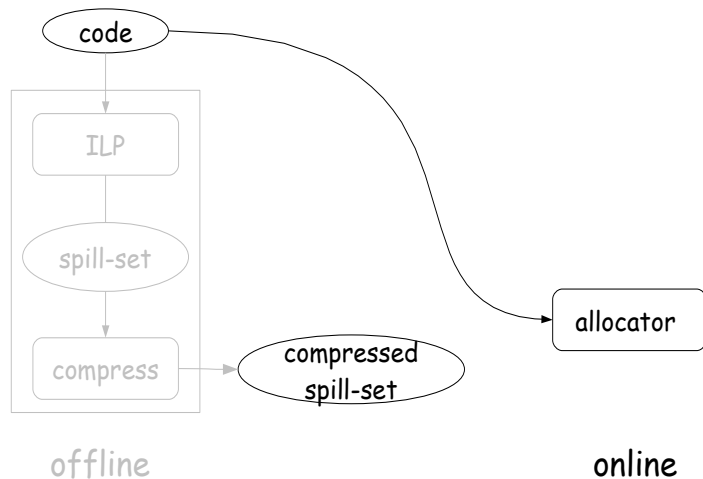


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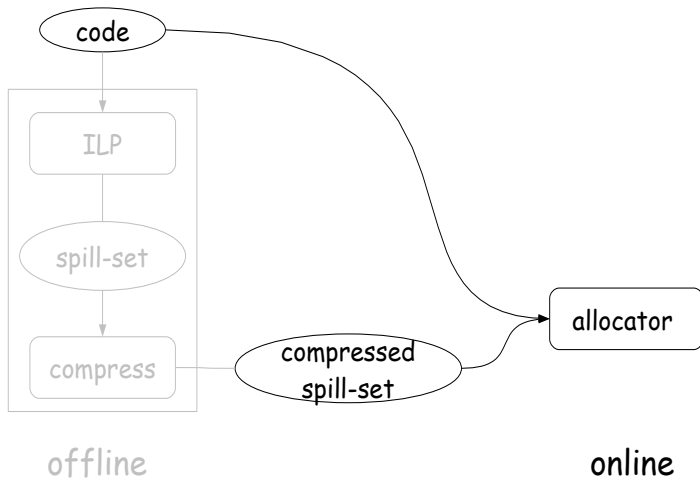




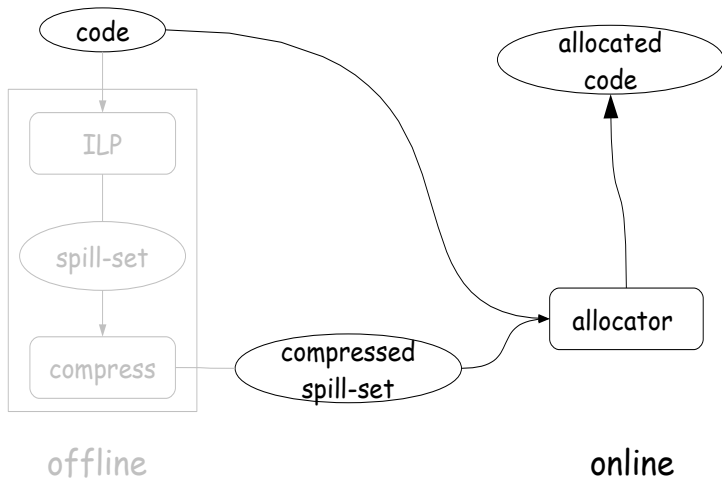
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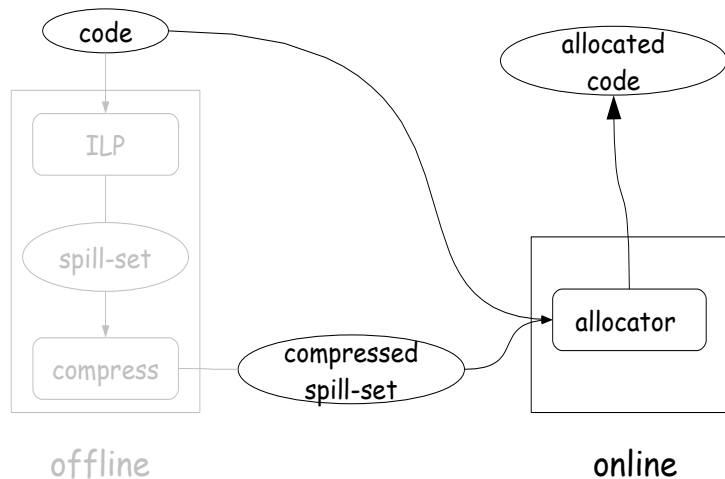
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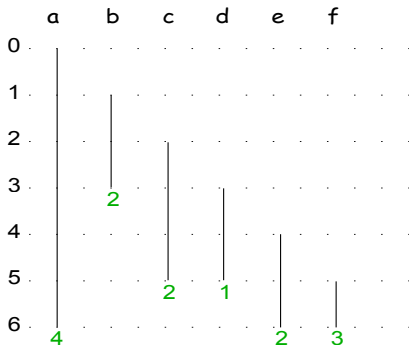
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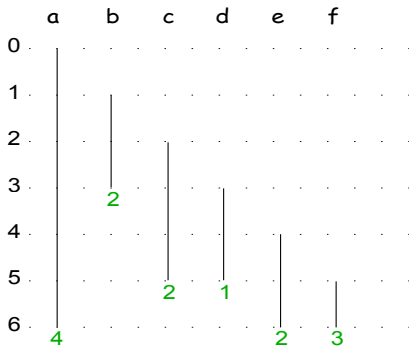
# COMPRESSION

- Spill-Set produced by ILP can be used as annotation
- But we want to reduce the annotation size
  - Run the online allocator
  - Drop from the annotation any spilled variable that would be found by the online allocator

# COMPRESSION ALGORITHM

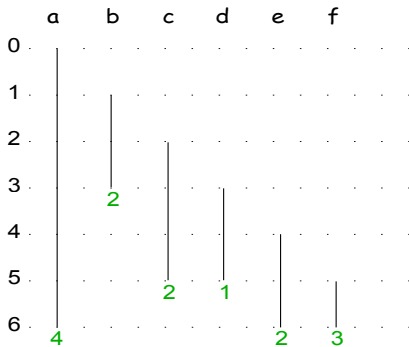


# COMPRESSION ALGORITHM



2 available  
registers

# COMPRESSION ALGORITHM

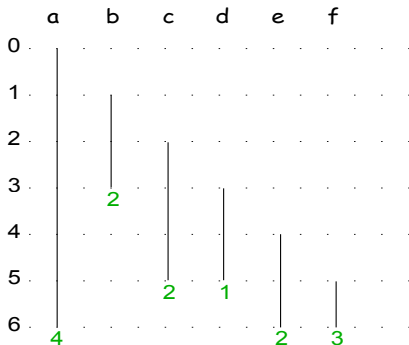


2 available  
registers

Optimal spill-set:  
{c,e}



# COMPRESSION ALGORITHM

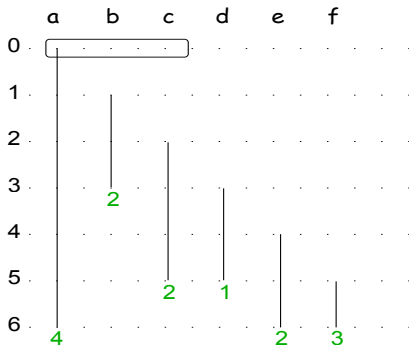


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM

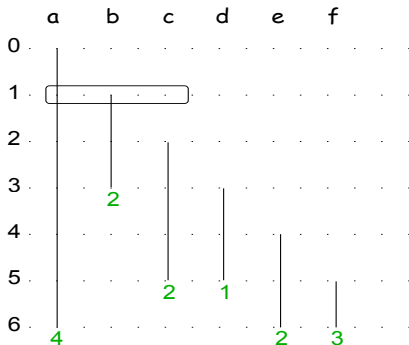


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM

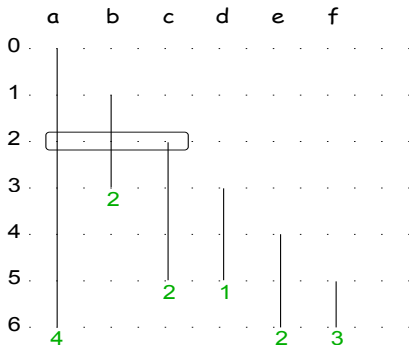


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM

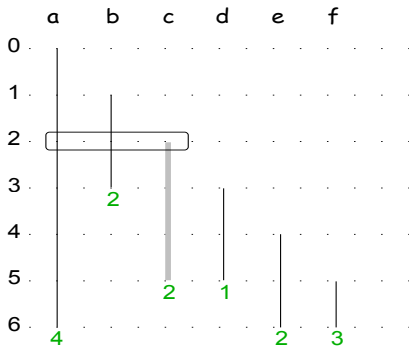


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM

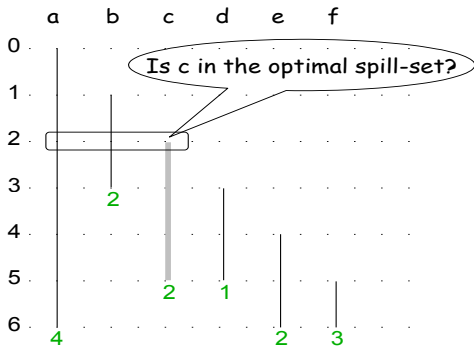


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM

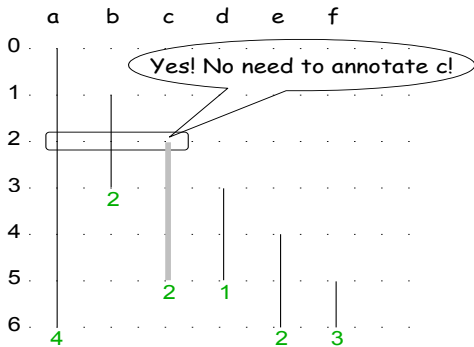


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM

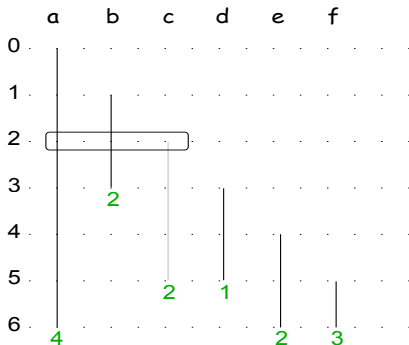


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM



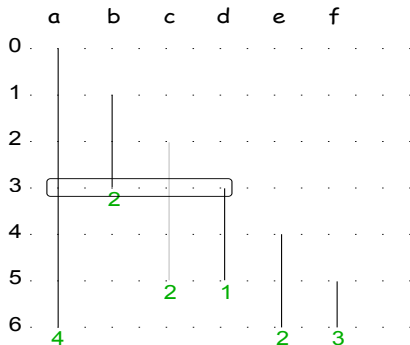
2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:



# COMPRESSION ALGORITHM

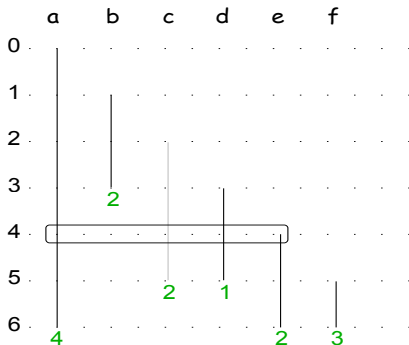


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM

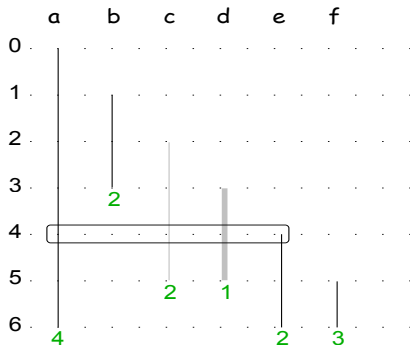


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM

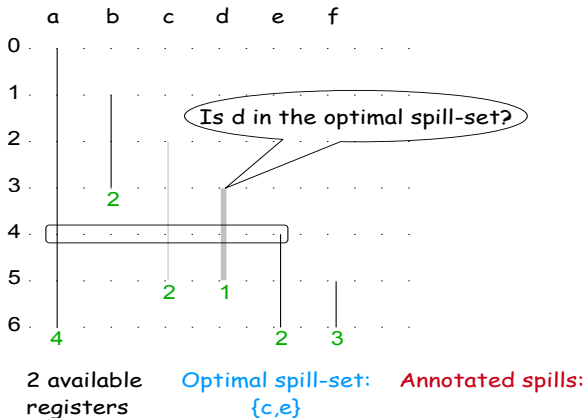


2 available  
registers

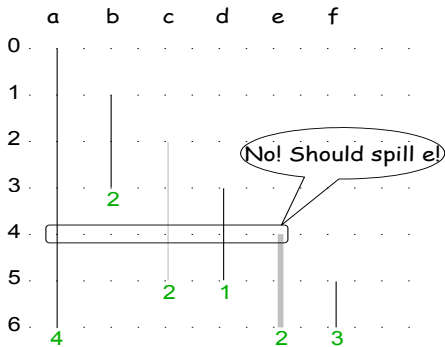
Optimal spill-set:  
{c,e}

Annotated spills:

# COMPRESSION ALGORITHM



# COMPRESSION ALGORITHM

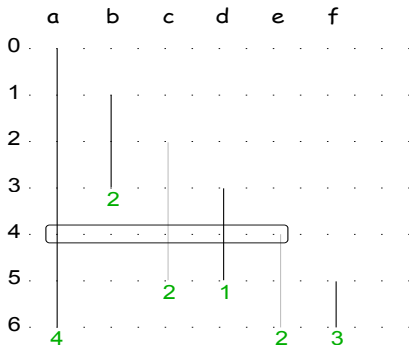


2 available  
registers

Optimal spill-set:  
 $\{c, e\}$

Annotated spills:

# COMPRESSION ALGORITHM

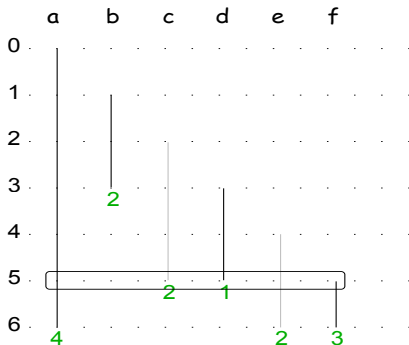


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:  
{e}

# COMPRESSION ALGORITHM

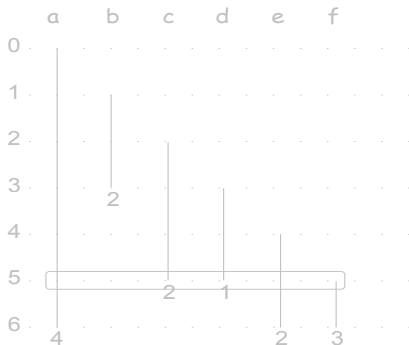


2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:  
{e}

# COMPRESSION ALGORITHM



2 available  
registers

Optimal spill-set:  
{c,e}

Annotated spills:  
{e}



# EXPERIMENTS: FRAMEWORK

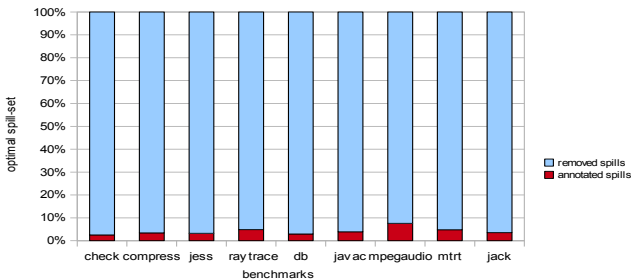
## FRAMEWORK:

- JikesRvm 3.0.1
- CPLEX
- SPEC JVM98 benchmarks

# EXPERIMENTS: ANNOTATION

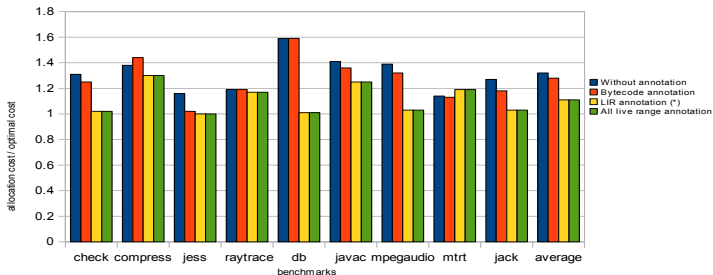
- Preserving the information collected in the offline stage requires at most 0.26% of the live ranges to be annotated

# EXPERIMENTS: COMPRESSION



compression rate

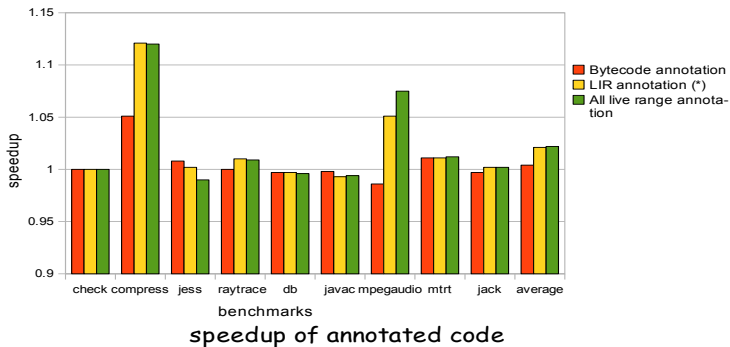
# EXPERIMENTS: ALLOCATION COST



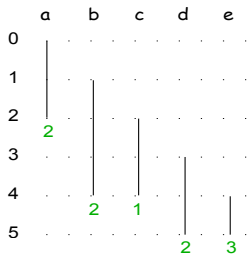
split compilation cost w.r.t. optimal cost

lower is better

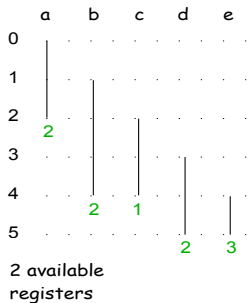
# EXPERIMENTS: SPEEDUPS



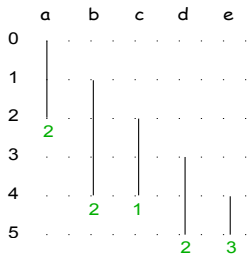
# PORTABILITY IN REGISTER COUNTS 1/2



# PORTABILITY IN REGISTER COUNTS 1/2



# PORTABILITY IN REGISTER COUNTS 1/2

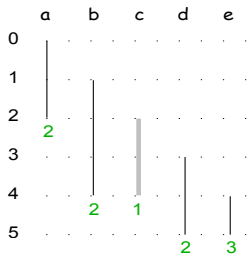


2 available  
registers

Optimal spill-set =



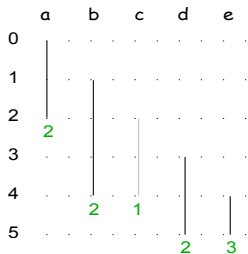
# PORTABILITY IN REGISTER COUNTS 1/2



2 available  
registers

Optimal spill-set =

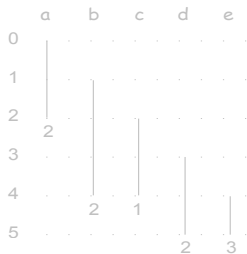
# PORTABILITY IN REGISTER COUNTS 1/2



2 available  
registers

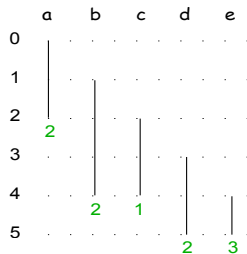
Optimal spill-set = {c}

# PORTABILITY IN REGISTER COUNTS 1/2

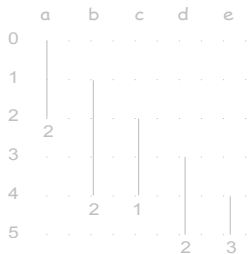


2 available registers

Optimal spill-set = {c}

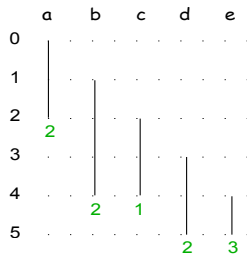


# PORTABILITY IN REGISTER COUNTS 1/2



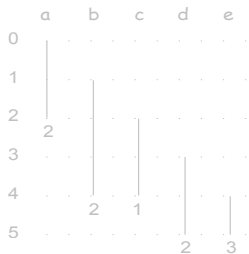
2 available registers

Optimal spill-set = {c}



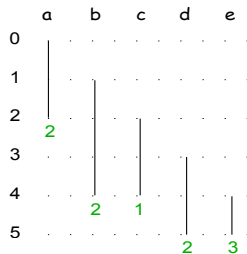
1 available register

# PORTABILITY IN REGISTER COUNTS 1/2



2 available registers

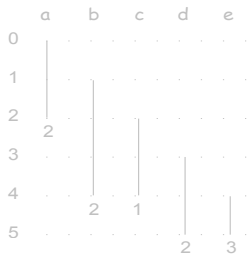
Optimal spill-set = {c}



1 available register

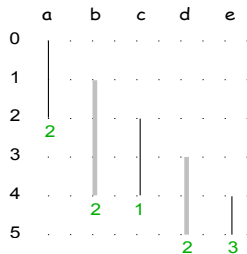
Optimal spill-set =

# PORTABILITY IN REGISTER COUNTS 1/2



2 available registers

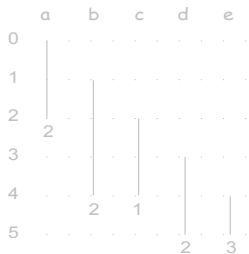
Optimal spill-set = {c}



1 available register

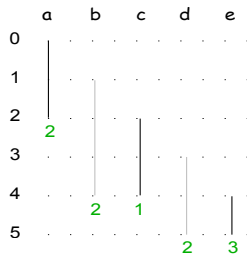
Optimal spill-set =

# PORTABILITY IN REGISTER COUNTS 1/2



2 available  
registers

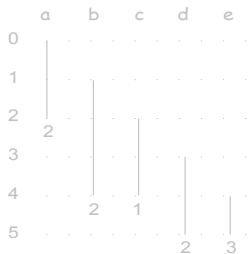
Optimal spill-set = {c}



1 available  
register

Optimal spill-set = {b,d}

# PORTABILITY IN REGISTER COUNTS 1/2



2 available registers

Optimal spill-set = {c}

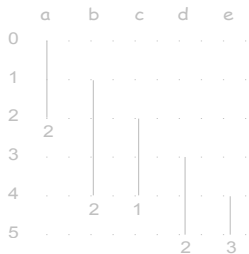


1 available register

Optimal spill-set = {b,d}



# PORTABILITY IN REGISTER COUNTS 1/2



2 available  
registers

Optimal spill-set = {c}

$\{c\} \not\subseteq \{b,d\}$



1 available  
register

Optimal spill-set = {b,d}

# PORTABILITY IN REGISTER COUNTS 2/2

## EXPERIMENTAL STUDY

- Varying the number of registers from 2
- ... to the maximal number where spilling is needed

## RESULT

- Inclusion property holds for **99.83%** of the SPEC JVM98's methods

# SEPARATE COMPILATION

What is the impact of calling an annotated code that will be :

# SEPARATE COMPILATION

What is the impact of calling an annotated code that will be :

- later inlined

# SEPARATE COMPILATION

What is the impact of calling an annotated code that will be :

- later inlined
- later called from a different context

# SEPARATE COMPILATION

What is the impact of calling an annotated code that will be :

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## 1. Most frequent calling context

# SEPARATE COMPILATION

What is the impact of calling an annotated code that will be :

- later inlined
  - later called from a different context
- 
1. Most frequent calling context
  2. Multi-versionning depending on the calling context

# CONCLUSION

Recipe for split compilation success:

1. What can be done offline?
2. What should be done online?
3. Leverage fundamental algorithmic results to coordinate the two stages
  - live range splitting
  - maxlive colorability criterion



# REFERENCES



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Register allocation: What does the NP-completeness proof of Chaitin et al. really prove?